## Source and Accuracy of Estimates for Money Income in the United States: 2001

## **SOURCES OF DATA**

Most estimates in this report come from data obtained in March of years 1968 through 2002 in the Current Population Survey (CPS). The survey is conducted every month, although this report uses only March data for its estimates. The March survey uses two sets of questions, the basic CPS and the supplement.

Data was used from various sources in developing alternative measures of income for 2001. Specifically, data from the American Housing Survey (AHS), the Income Survey Development Program (ISDP), and the Internal Revenue Service (IRS) with CPS data to create simulations of taxes paid, number of tax filing units, adjusted gross income, and other tax characteristics was combined for the March 2002 CPS.

In addition, this report uses the *State Tax Handbook* from the Commerce Clearing House as an information source for tax data. For noncash valuation estimates, this report uses data from the U.S. Department of Agriculture (USDA), the Health Care Financing Administration (HCFA), and the Department of Housing and Urban Development (HUD).

A description of the sources of data we used to derive these estimates follows. Except for the CPS, these descriptions are brief. See Current Population Reports, Series P60-186RD, *Measuring the Effect of Benefits and Taxes on Income and Poverty: 1992*, and publications on the appropriate surveys for more details.

American Housing Survey. Housing data was collected for the Department of Housing and Urban Development. The population covered by the sample for the AHS (called the Annual Housing Survey before 1984) includes all housing units in the United States. For a more detailed description of the sample design, see the report Current Housing Reports, Series H150-89, The American Housing Survey for the United States in 1989, U.S. Department of Commerce.

The AHS is no longer conducted in even-numbered years, so the property tax estimates in this report are based on the 1995 AHS. Also, for the noncash estimates, the 1985 AHS data was used in a model to estimate the value of public housing. For more details on

the AHS model used to estimate public and subsidized housing values, please see Appendix B of Current Population Reports, Series P60-186RD, Measuring the Effect of Benefits and Taxes on Income and Poverty: 1992.

Income Survey Development Program. The ISDP was the research and development phase for the Survey of Income and Program Participation (SIPP). The ISDP was used to examine and resolve design, operational, and technical issues for SIPP. The household sample for the 1979 ISDP was a nationwide, multiple-frame sample. The majority of sample households in the ISDP came from addresses contacted in the 1976 Survey of Income and Education. Statisticians selected the remainder of sample households from a reserve file of sample cases maintained by the Census Bureau. For a more detailed description of this sample design, see the report Wage and Salary Data From the Income Survey Development Program: 1979 (Preliminary Data From Interview Period One), Current Population Reports, Special Studies, Series P-23, No. 118.

Internal Revenue Service Data. Much of the IRS data in this report came from the Statistics of Income (SOI) series, in particular the SOI Bulletin *Individual Income Tax Returns, Preliminary Data: 2000,* Spring 2002. This report, based on a sample drawn from all tax returns filed in 2001, presents information on taxpayers' incomes, exemptions, deductions, credits, and taxes.

**Data From Other Sources**. The *State Tax Handbook*, October 1, 1991, from the Commerce Clearing House, includes information on state tax systems. These data were updated to reflect changes in state income tax rates.

Much of the data on cash and noncash benefits are from administrative records. Values of school lunches and food stamps are from USDA unpublished data. Medicaid and medicare data come from HCFA unpublished records. Also, USDA and HUD data are used to compute medicaid and medicare values. For more details, see Appendix B of Current Population Reports, Series P60- 186RD, Measuring the Effect of Benefits and Taxes on Income and Poverty: 1992.

Table E-1. **Description of the March Current Population Survey** 

Time posied	Number of	Housing units eligible <sup>1</sup>		
Time period	sample areas	Interviewed	Not interviewed	
1996 to 2002	754	46,800	3,200	
1995	792	56,700	3,300	
1990 to 1994	729	57,400	2,600	
1989	729	53,600	2,500	
1986 to 1988	729	57,000	2,500	
1985	<sup>2</sup> 629/729	57,000	2,500	
1982 to 1984	629	59,000	2,500	
1980 to 1981	629	65,500	3,000	
1977 to 1979	614	55,000	3,000	
1973 to 1976	461	46,500	2,500	
1972	449	45,000	2,000	
1968 to 1971	449	48,000	2,000	

<sup>&</sup>lt;sup>1</sup>Excludes about 12,500 households added due to the SCHIP sample expansion, 1,300 of which are not interviewed. (See "CPS March Supplement.")

<sup>2</sup>The Census Bureau redesigned the CPS following the 1980 Decennial Census of Population and Housing. During phase-in of the new design, housing units from the new and old designs were in the sample.

Source: U.S. Census Bureau, Demographic Statistical Methods Division.

**Basic CPS**. The monthly CPS collects primarily labor force data about the civilian noninstitutional population. Interviewers ask questions concerning labor force participation about each member 15 years old and over in every sample household.

**CPS March Supplement**. In March 2002, the interviewers asked additional questions about money income received the previous calendar year.

Basic CPS Sample. The present monthly CPS sample was selected from the 1990 decennial Census files with coverage in all 50 states and the District of Columbia. The sample is continually updated to account for new residential construction. To obtain the sample, the United States is divided into 2,007 geographic areas. In most states, a geographic area consisted of a county or several contiguous counties. In some areas of New England and Hawaii, minor civil divisions are used instead of counties. These 2,007 geographic areas were then grouped into 754 strata, and one geographic area was selected from each stratum.

About 60,000 occupied households are eligible for interview every month out of the 754 strata. Interviewers are unable to obtain interviews at about 4,500 of these units. This occurs when the occupants are not found at home after repeated calls or are unavailable for some other reason.

The number of households that are eligible for interview in the basic CPS increased from 50,000 in 2000 to 60,000 in July of 2001. This increase in the number of eligible households is due to the implementation of the State Children's Health Insurance Program

(SCHIP) sample expansion. The SCHIP sample expansion increased the monthly CPS sample in states with high sampling errors for low-income uninsured children. With this increase in eligible households, the number of units where interviewers were unable to obtain an interview increased from 3,200 to 4,500.

CPS March Supplement Sample. To obtain more reliable data for certain minority groups, the March Supplement sample includes 21,000 eligible housing units in addition to the 60,000 eligible housing units from the basic CPS. Included in this 21,000 housing unit increase are Hispanic¹ households in sample from the previous November and following April, non-Hispanic non-White households in sample from the previous November, and non-Hispanic White households with children under 19 years of age in sample from in the previous November and following April. This March Supplement sample increase of 21,000 was first included in March 2001 for testing purposes and in March 2002 for reporting purposes.

CPS Sample Redesign. Since the introduction of the CPS, the Census Bureau has redesigned the CPS sample several times. These redesigns have improved the quality and accuracy of the data and have satisfied changing data needs. The most recent changes were phased in and implementation was completed in 1995.

Table E-1 summarizes changes in the CPS designs for the years for which data appear in this report.

<sup>&#</sup>x27;This report shows information on the Hispanic population collected in the 50 states and the District of Columbia, and therefore, does not include residents of Puerto Rico. Hispanics may be of any race.

**CPS Estimation Procedure.** This survey's estimation procedure adjusts weighted sample results to agree with independent estimates of the civilian noninstitutional population of the United States by age, sex, race, and Hispanic/non-Hispanic ancestry, and state of residence. The adjusted estimate is called the post-stratification ratio estimate. The independent estimates are calculated based on information from three primary sources:

- The 2000 Decennial Census of Population and Housing.
- Statistics on births, deaths, immigration, and emigration.
- Statistics on the size of the armed forces.

The independent population estimates used for 2002 (income estimates for 2001) are based on updates to controls established by the 2000 decennial census. The 1994 to 2001 population estimates (income estimates for 1993 to 2000) are based on updates to controls established by the 1990 decennial census. Data previous to 1994 are based on independent population estimates from the latest available decennial census data.

The estimation procedure for the March supplement included a further adjustment so husband and wife of a household received the same weight. The independent population estimates include some, but not all, undocumented immigrants.

## **ACCURACY OF ESTIMATES**

A sample survey estimate has two possible types of error: nonsampling and sampling. The accuracy of an estimate depends on both types of error. The nature of the sampling error is known given the survey design. The full extent of the nonsampling error, however, is unknown. Consequently, one should be particularly careful when interpreting results based on a relatively small number of cases or on small differences between estimates.

**Sampling Error**. Since the CPS estimates come from a sample, they may differ from figures from a complete census using the same questionnaires, instructions, and enumerators. This possible variation in the estimates due to sampling error is known as "sampling variability."

To estimate the standard error of a CPS estimate, the Census Bureau uses replicated variance estimation methods. These methods primarily measure the magnitude of sampling error. However, they do measure

some effects of nonsampling error as well. They do not measure systematic biases in the data due to nonsampling error. (Bias is the average over all possible samples of the differences between the sample estimates and the true value.)

**Nonsampling Error**. Nonsampling errors can be attributed to several sources including the following:

- Inability to obtain information about all cases in the sample (nonresponse).
- Definitional difficulties.
- Differences in the interpretation of questions.
- Respondent inability or unwillingness to provide correct information.
- Respondent inability to recall information.
- Errors made in data collection, such as in recording or coding the data.
- Errors made in processing the data.
- Errors made in estimating values for missing data.
- Failure to represent all units with the sample (undercoverage).

Answers to questions about money income often depend on the memory or knowledge of one person in a household. Recall problems can cause underestimates of income in survey data, because it is easy to forget minor or irregular sources of income. Respondents may also misunderstand what the Census Bureau considers money income or may simply be unwilling to answer these questions correctly because the questions are considered too personal. See Appendix C, Current Population Reports, Series P60-184, Money Income of Households, Families, and Persons in the United States: 1992 for more details.

For additional information on nonsampling error including the possible impact on CPS data when known, refer to:

- Statistical Policy Working Paper 3, An Error Profile: Employment as Measured by the Current Population Survey, Office of Federal Statistical Policy and Standards, U.S. Department of Commerce, 1978.
- Technical Paper 63RV, The Current Population Survey: Design and Methodology, U.S. Census Bureau, U.S. Department of Commerce, 2002.

**Undercoverage**. CPS undercoverage results from missed housing units and missed people within

Table E-2.

March CPS Coverage Ratios

A 70	Non-Black		Black		All races		
Age	Male	Female	Male	Female	Male	Female	Total
0 to 14 years	0.942	0.951	0.880	0.904	0.932	0.943	0.937
15 to 19 years	0.864	0.910	0.885	0.751	0.867	0.884	0.876
20 to 24 years	0.823	0.877	0.707	0.757	0.808	0.859	0.834
25 to 29 years	0.863	0.919	0.755	0.810	0.850	0.903	0.877
30 to 34 years	0.880	0.950	0.671	0.833	0.855	0.934	0.895
35 to 44 years	0.899	0.940	0.684	0.863	0.875	0.930	0.903
45 to 54 years	0.938	0.961	0.778	0.953	0.923	0.960	0.942
55 to 64 years	0.932	0.953	0.834	0.929	0.923	0.951	0.938
65 to 74 years	0.932	0.977	0.939	0.958	0.932	0.975	0.956
75 years and older	1.019	1.008	0.910	0.961	1.011	1.004	1.007
15 years and older	0.902	0.945	0.767	0.858	0.887	0.934	0.912
0 years and older	0.911	0.946	0.802	0.871	0.898	0.936	0.917

Source: U.S. Census Bureau, Demographic Statistical Methods Division.

sample households. Overall CPS undercoverage is estimated to be about 8 percent. CPS Undercoverage varies with age, sex, and race. Generally, undercoverage is larger for males than for females and larger for Blacks and other races combined than for Whites.

The Current Population Survey weighting procedure uses ratio estimation whereby sample estimates are adjusted to independent estimates of the national population by age, race, sex and Hispanic ancestry. This weighting partially corrects for bias due to undercoverage, but biases may still be present when people who are missed by the survey differ from those interviewed in ways other than age, race sex, and Hispanic ancestry. How this weighting procedure affects other variables in the survey is not precisely known. All of these considerations affect comparisons across different surveys or data sources.

A common measure of survey coverage is the coverage ratio, the estimated population before post-stratification divided by the independent population control. Table E–2 shows CPS coverage ratios for age-sex-race groups for a typical month. The CPS coverage ratios can exhibit some variability from month to month, but these are a typical set of coverage ratios.

**Comparability of Data**. Data obtained from the CPS and other sources are not entirely comparable. This results from differences in interviewer training and experience and in differing survey processes. This is an example of nonsampling variability not reflected in the standard errors. Therefore, caution should be used when comparing results from different sources.

A number of changes were made in data collection and estimation procedures beginning with the January

1994 CPS. The major change was the use of a new questionnaire. The questionnaire was redesigned to measure the official labor force concepts more precisely, to expand the amount of data available, to implement several definitional changes, and to adapt to a computer-assisted interviewing environment. The March supplemental income questions were also modified for adaptation to computer-assisted interviewing, although there were no changes in definitions and concepts. Due to these and other changes, one should use caution when comparing estimates from data collected before 1994 with estimates from data collected in 1994 and later.

Data users should also use caution when comparing CPS estimates in this report, which reflect 2000 census-based population controls, with estimates for 1993 to 2000 (from March 1994 CPS to March 2001 CPS), which reflect 1990 census-based population controls and with estimates for 1992 (from March 1993 CPS)and earlier years, which reflect 1980 census-based population controls. Although this change in population controls had relatively little impact on summary measures, such as means, medians, and percentage distributions, it did have a significant impact on levels. For example, use of 2000 based population controls results in about a one percent increase from the 1990 based population controls in the civilian noninstitutional population and in the number of families and households. Thus, estimates of levels for data collected in 2002 and later years will differ from those for earlier years by more than what could be attributed to actual changes in the population. These differences could be disproportionately greater for certain subpopulation groups than for the total population.

Table E-3. CPS Standard Error Parameters for Income and Nonincome Characteristics: 2001

Characteristic	Total o	r White	Black		Hispanic	
Characteristic	а	b	а	b	а	b
ALL INCOME LEVELS						
People						
Total	-0.000006 -0.000012 -0.000011	1,249 1,249 1,249	-0.000055 -0.000123 -0.000099	1,430 1,430 1,430	-0.000054 -0.000104 -0.000108	1,430 1,430 1,430
Age						
15 to 24 years	-0.000032 -0.000015 -0.000019 -0.000037	1,249 1,249 1,249 1,249	-0.000247 -0.000137 -0.000204 -0.000511	1,430 1,430 1,430 1,430	-0.000141 -0.000080 -0.000089 -0.000270	1,430 1,430 1,430 1,430
Housheold, Families, and Unrelated Individuals						
Total	-0.000005	1,140	-0.000048	1,245	-0.000047	1,245
NONINCOME CHARACTERISTICS						
People						
Employment Status Educational Attainment	-0.000008 -0.000005	1,586 1,206	-0.000154 -0.000052	3,296 1,364	-0.000187 -0.000035	3,296 922
Marital Status, Household and Family Characteristics						
Some household members	-0.000009 -0.000011	2,652 3,222	-0.000106 -0.000156	3,809 5,617	-0.000102 -0.000150	3,809 5,617
Households, Families, and Unrelated Individuals						
Total	-0.000005	1,052	-0.000036	952	-0.000036	952

Notes: To obtain parameters prior to 2001, multiply by the appropriate factor in Table E-4.

For nonmetropolitan residence categories multiply the a and b parameters by 1.5.

For foreign-born noncitizen characteristics for Total and White, multiply the a and b parameters by 1.3. No adjustment is necessary for foreign-born and noncitizen characteristics for Blacks and Hispanics.

For regional estimates, multiply the a and b parameters by 0.89, 0.91, 1.14, and 1.23 for Northeast, Midwest, South, and West, respectively.

Source: U.S. Census Bureau, Demographic Statistical Methods Division.

Caution should also be used when comparing Hispanic estimates over time. No independent population control totals for people of Hispanic ancestry were used before 1985.

Based on the results of each decennial census, the Census Bureau gradually introduces a new sample design for the CPS. During this phase-in period, CPS data are collected from sample designs based on different censuses. While most CPS estimates were unaffected by this mixed sample, geographic estimates are subject to greater error and variability. Users should exercise caution when comparing estimates across years for metropolitan/nonmetropolitan categories. For more information, see Appendix C, Current Population Reports, Series P60-193, Money Income in the United States: 1995 (With Separate Data on Valuation of Noncash Benefits).

Note When Using Small Estimates. Summary measures (such as medians, means, and percentage distributions) are shown only when the base is 75,000 or greater. Because of the large standard errors involved, summary measures would probably not reveal useful information when computed on a smaller base. However, estimated numbers are displayed even though the relative standard errors of these numbers are larger than those for corresponding percentages. These smaller estimates permit combinations of the categories to suit data users' needs. Take care in the interpretation of small differences. For instance, even a small amount of nonsampling error can cause a borderline difference to appear significant or not, thus distorting a seemingly valid hypothesis test.

**Estimation of Median Incomes**. The methodology for computing median income has changed over the

past few years. Medians were computed using either Pareto interpolation or linear interpolation. Currently, linear interpolation is used to estimate all medians. Pareto interpolation assumes a decreasing density of population within an income interval; whereas, linear interpolation assumes a constant density of population within an income interval. Estimates of median income for 1979 through 1987 and associated standard errors were calculated using Pareto interpolation if the estimate was larger than \$20,000 for people or \$40,000 for families and households. This is because the width of the income interval containing the estimate is greater than \$2,500.

Estimates of median income for 1976, 1977, and 1978 and associated standard errors were calculated using Pareto interpolation if the estimate was larger than \$12,000 for people or \$18,000 for families and households. This is because the width of the income interval containing the estimate is greater than \$1,000. All other estimates of median income and associated standard errors for 1976 through 2001 and almost all of the estimates of median income and associated standard errors for 1975 and earlier were calculated using linear interpolation.

Thus, use caution when comparing median incomes above \$12,000 for people or \$18,000 for families and households for different years. Median incomes below those levels are more comparable from year to year since they have always been calculated using linear interpolation. For an indication of the comparability of medians calculated using Pareto interpolation with medians calculated using linear interpolation, see Series P-60, No. 114, *Money Income in 1976 of Families and Persons in the United States*.

**Standard Errors and Their Use**. The sample estimate and its standard error enable one to construct a confidence interval. A confidence interval is a range that would include the average result of all possible samples with a known probability. For example, if all possible samples were surveyed under essentially the same general conditions and using the same sample design, and if an estimate and its standard error were calculated from each sample, then approximately 90 percent of the intervals from 1.645 standard errors below the estimate to 1.645 standard errors above the estimate would include the average result of all possible samples.

Data users must use a number of approximations to derive, at a moderate cost, standard errors applicable to all the estimates in this report. Instead of providing an individual standard error for each estimate, two

Table E-4.

CPS Factors to Apply to a and b Parameters for Estimates Prior to 2001

Characteristic	Factor
NON-HISPANIC	
1995 to 2000 1989 to 1994 1988	1.96 1.80 2.00 1.69 1.47
HISPANIC	
1995 to 2000 1989 to 1994 1988 1984 to 1987	1.96 1.80 2.33 1.47

Source: U.S. Census Bureau, Demographic Statistical Methods Division.

parameters, a and b, have been provided to calculate standard errors for each type of characteristic.

Table E–3 has CPS standard error parameters for income and various nonincome characteristics. Table E–4 provides factors to approximate CPS standard error parameters for estimates before 2001. Table E–5 provides CPS Hispanic parameters for estimates before 1984. Table E–6 provides CPS parameters for income and various nonincome characteristics for Asian and Pacific Islanders and American Indian and Alaskan Natives. Table E–7 contains the year-to-year CPS correlation coefficients for income characteristics.

A particular confidence interval may or may not contain the average estimate derived from all possible samples. However, one can say with specified confidence that the interval includes the average estimate calculated from all possible samples.

Standard errors may be used to perform hypothesis testing. This is a procedure for distinguishing between population parameters using sample estimates. The most common type of hypothesis appearing in this report is that two population parameters are different. An example of this would be comparing the median annual income of Black families with the median annual income of White non-Hispanic families.

Tests may be performed at various levels of significance. A significance level is the probability of concluding that the characteristics are different when, in fact, they are the same. All statements of comparison in the text were tested at the 0.10 level of significance or better. This means that the absolute value of the estimated difference between characteristics is greater

Table E-5. **CPS Standard Error Parameters for Income and Nonincome Characteristics** of Hispanics: 1972 to 1983

Characteristic	1972	-1980	1981-1983		
Characteristic	а	b	а	b	
ALL INCOME LEVELS					
People					
Total	-0.000020 -0.000043 -0.000038	3,000 3,000 3,000	-0.000301 -0.000615 -0.000591	3,357 3,357 3,357	
Age					
15 to 24 years	-0.000080 -0.000065 -0.000077 -0.000147 (X)	3,000 3,000 3,000 3,000 (X)	-0.000961 -0.000668 -0.001459 -0.004124 (X)	3,357 3,357 3,357 3,357 (X)	
Household, Families, and Unrelated Individuals					
Total	-0.000014 (X) -0.000014	2,420 (X) 2,420	-0.000237 (X) -0.000237	2,708 (X) 2,708	
NONINCOME CHARACTERISTICS					
People					
Employment status	(X) -0.000015 (X)	(X) 2,344 (X)	-0.000152 (X)	(X) 2,623 (X)	
Total, Marital Status, Other					
Some household members	-0.000026 -0.000044	5,069 10,199	-0.000294 -0.000592	5,673 11,414	
Households, Families, and Unrelated Individuals					
Total	-0.000020 (X)	1,626 (X)	-0.000022 (X)	1,820 (X)	

X Not applicable.

Note: Data users should multiply the a and b parameters by 1.5 for nonmetropolitan residence categories. The Census Bureau did not publish income data for Hispanics before 1972.

Source: U.S. Census Bureau, Demographic Statistical Methods Division.

than or equal to 1.645 times the standard error of the difference.

Standard Errors of Estimated Numbers. The approximate standard error, sx, of an estimated number shown in this report can be obtained using the formula

$$s_x = \sqrt{ax^2 + bx} \tag{1}$$

Here

x is the size of the estimate and a and b are the parameters in Table E-3 or E-6 associated with the particular type of characteristic. When calculating

standard errors for numbers from cross-tabulations involving different characteristics, use the set of parameters for the characteristic which will give the largest standard error.

Illustration. There were 74,386,000 family households in 2002. Use the appropriate parameters from Table E-3 and formula (1) to get

74,386,000 Estimate, x a parameter -0.000005 b parameter 1,052 225,000 Standard error

90% confidence interval 74,016,000 to 74,756,000

Table E-6.

CPS Standard Error Parameters for Income and Nonincome Characteristics of Asians and Pacific Islanders and American Indians and Alaskan Natives: 2001

Characteristic	а	b
ALL INCOME LEVELS		
People Households, families, and unrelated individuals	-0.000116 -0.000101	1,430 1,245
NONINCOME CHARACTERISTICS		
People		
Marital status, household and family characteristics: Some household members	-0.000238 -0.000351	3,809 5,617
Households, families, and unrelated individuals	-0.000077	952

Note: To obtain parameters prior to 2001, multiply by the appropriate factor in Table E-4. Income data for Asians and Pacific Islanders and American Indians and Alaskan Natives were not collected prior to 1988.

Source: U.S. Census Bureau, Demographic Statistical Methods Division.

The standard error is calculated as

$$s_{y} = \sqrt{(-0.000005)(74,386,000)^{2} + (1,052)(74,386,000)} = 225,000$$

The 90-percent confidence interval for the estimated number of family households in 2002 is calculated as  $74,386,000 \pm 1.645 \times 225,000$ .

A conclusion that the average estimate derived from all possible samples lies within a range computed in this way would be correct for roughly 90 percent of all possible samples.

**Standard Errors of Estimated Percentages**. The reliability of an estimated percentage, computed using sample data from both numerator and denominator, depends on the size of the percentage and its base. Estimated percentages are relatively more reliable than the corresponding estimates of the numerators of the percentages, particularly if the percentages are 50 percent or more. When the numerator and denominator of the percentage are in different categories, use the parameter from Table E–3 or E–6 indicated by the numerator.

The approximate standard error, sx,p, of an estimated percentage is approximately equal to

$$s_{x,p} = \sqrt{\frac{b}{x}p(100-p)}$$
 (2)

Here x is the total number of people, families, households, or unrelated individuals in the base of the percentage, p is the percentage (0 p 100), and b is the parameter in Table E-3 or E-6 associated with the characteristic in the numerator of the percentage.

**Illustration**. There were 13,155,000 or 17.7 percent of the 74,386,000 family households maintained by female householders with no husband present. Use the appropriate parameter from Table E–3 and formula (2) to get

17.7
74,386,000
1,052
0.14
7.5 to 17.9

The standard error is calculated as

$$s_{x,y} = \sqrt{\frac{1,052}{74,386,000} (17.7)(100 - 17.7)} = 0.14$$

The 90-percent confidence interval for the estimated percentage of family households that were maintained by female householders with no husband present is calculated as  $17.7 \pm 1.645 \times 0.14$ .

**Standard Error of a Difference**. The standard error of the difference between two sample estimates is approximately equal to

$$s_{x-y} = \sqrt{s_x^2 + s_y^2 - 2rs_x s_y}$$
 (3)

where s<sub>X</sub> and s<sub>y</sub> are the standard errors of the estimates, x and y. The estimates can be numbers, percentages, ratios, etc. Table E–7 contains the correlation coefficient, r, for year-to-year comparisons for CPS income estimates of numbers and proportions. This will represent the actual standard error quite accurately for the difference between estimates of the same

Table E-7. **CPS Year-to-Year Correlation Coefficients** for Income Estimates: 1960 to 2001

	1960-2001  Famili househol a unrela People individu	
Characteristic		
Total	0.30	0.35
White	0.30 0.30 0.30 0.45	0.35 0.35 0.35 0.55

<sup>&</sup>lt;sup>1</sup>Hispanics may be of any race.

Note: These correlations are for comparisons of consecutive years. For comparisons of nonconsecutive years, assume the correlations are zero. For Asians and Pacific Islanders and American Indians and Alaskan Natives, use the correlation coefficient for total.

Source: U.S. Census Bureau, Demographic Statistical Methods Division.

characteristic in two different areas, or for the difference between separate and uncorrelated characteristics in the same area. However, if there is a high positive (negative) correlation between the two characteristics, the formula will overestimate (underestimate) the true standard error.

**Illustration**. The median earnings of all male fulltime, year-round workers in 2001, x, was \$38,256 and the median earnings of all female full-time, year-round workers in 2001, y, was \$29,210. The apparent difference between the median income of males and females in 2001 was \$9,046. The approximate standard errors, sx and sy, are \$258 and \$165, respectively. Use formula (3) with r = 0 to get

	Х	У	difference
Estimate	\$38,256	\$29,210	\$9,046
Standard error	\$258	\$165	\$306
90% confidence	\$37,832 to	\$28,939 to	\$8,543 to
interval	\$38,680	\$29,481	\$9,549

The standard error of the difference is calculated as

$$s_{x-y} = \sqrt{(258)^2 + (165)^2} = 306$$

The 90-percent confidence interval for the estimated difference between the median income of male and female full-time, year-round workers in 2001 is calculated as  $$9,046 \pm 1.645 \times $306$ . Because this interval does not contain zero, we can conclude with 90-percent confidence that the median income of male full-time,

year-round workers in 2001 was larger than the median income of female full-time, year-round workers in 2001.

Standard Error of a Ratio. Certain estimates may be calculated as the ratio of two numbers. Compute the standard error of a ratio, x/y, using

$$s_{x/y} = \frac{x}{y} \sqrt{\left(\frac{s_x}{x}\right)^2 + \left(\frac{s_y}{y}\right)^2 - 2r \frac{s_x s_y}{xy}} \tag{4}$$

Calculate the standard error of the numerator, sx, and that of the denominator, sv, using formulas described earlier. In formula (4), r represents the correlation between the numerator and the denominator of the estimate. For one type of ratio, the denominator is a count of families or households and the numerator is a count of people in those families or households with a certain characteristic. If there is at least one person with the characteristic in every family or household, use 0.7 as an estimate of r. An example of this type is the mean number of children per family with children. For all other types of ratios, r is assumed to be zero. If r is actually positive (negative), then this procedure will provide an overestimate (underestimate) of the standard error of the ratio. Examples of this type are the mean number of children per family and the family poverty rate.

NOTE: For estimates expressed as the ratio of x per 100 y or x per 1,000 y, multiply formula (4) by 100 or 1,000, respectively, to obtain the standard error.

**Illustration**. The median earnings for full-time, year round female workers in 2001, x, was \$29,210 and the median earnings for full-time, year-round male workers in 2001, y, was \$38,256. The ratio of the median earnings is 0.76. The approximate standard errors,  $s_X$  and  $s_V$ , are \$165 and \$258, respectively. Using formula (4) with r = 0 to get

X	У	ratio
\$29,210	\$38,256	0.76
\$165	\$258	0.0067
\$28,939 to	\$37,832 to	0.75 to
\$29,481	\$38,680	0.77
	\$29,210 \$165 \$28,939 to	\$29,210 \$38,256 \$165 \$258 \$28,939 to \$37,832 to

The standard error is calculated as

$$s_{x/y} = \frac{29,210}{38,256} \sqrt{\left(\frac{165}{29,210}\right)^2 + \left(\frac{258}{38,256}\right)^2} = 0.0067$$

The 90-percent confidence interval for the ratio of the median earnings for full-time, year-round female

workers to the median earnings for full-time, year-round male workers is calculated as 0.76  $\pm$  1.645 x 0.0067.

**Standard Errors of Other Estimates**. This report provides standard errors for most estimates in the

respective tables, or includes a formula showing how to calculate them. For information on calculating other standard errors, contact Aneesah Stephenson at e-mail address:

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